

ANIMAL GENETICS & BREEDING

UNIT - I

BIO-STATISTICS AND COMPUTER
APPLICATION

Theory

Measure of Dispersion

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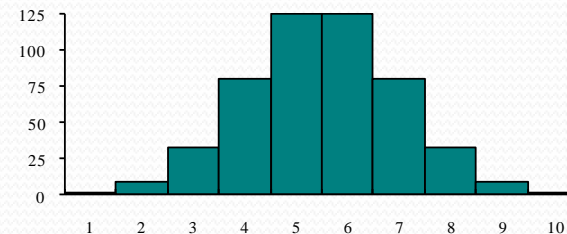
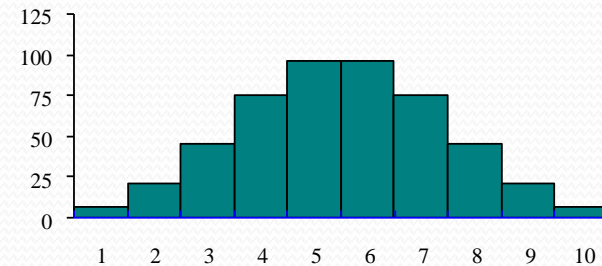
Measures of Dispersion

Definition

- *Measures of dispersion* are descriptive statistics that describe how similar a set of scores are to each other
 - The more similar the scores are to each other, the lower the measure of dispersion will be
 - The less similar the scores are to each other, the higher the measure of dispersion will be
 - In general, the more spread out a distribution is, the larger the measure of dispersion will be

Measures of Dispersion

- Which of the distributions of scores has the larger dispersion?
- ✚ The upper distribution has more dispersion because the scores are more spread out
 - ✚ That is, they are less similar to each other



Measures of Dispersion

- There are three main measures of dispersion:
 - Range
 - Variance
 - standard deviation

The Range

- The *range* is defined as the difference between the largest score in the set of data and the smallest score in the set of data, $X_L - X_S$
- What is the range of the following data:
4 8 1 6 6 2 9 3 6 9
- The largest score (X_L) is 9; the smallest score (X_S) is 1; the range is $X_L - X_S = 9 - 1 = 8$

When To Use the Range

- The range is used when
 - you have ordinal data or
 - you are presenting your results to people with little or no knowledge of statistics
- The range is rarely used in scientific work as it is fairly insensitive
 - It depends on only two scores in the set of data, X_L and X_S
 - Two very different sets of data can have the same range:
1 1 1 1 9 vs 1 3 5 7 9

Variance

- *Variance* is defined as the average of the square deviations:

$$\sigma^2 = \frac{\sum (X - \mu)^2}{N}$$

What Does the Variance Formula Mean?

- First, it says to subtract the mean from each of the scores
 - This difference is called a *deviate* or a *deviation score*
 - The deviate tells us how far a given score is from the typical, or average, score
 - Thus, the deviate is a measure of dispersion for a given score

What Does the Variance Formula Mean?

- Why can't we simply take the average of the deviates? That is, why isn't variance defined as:

$$\sigma^2 \neq \frac{\sum (X - \mu)}{N}$$

This is not the formula for variance!

What Does the Variance Formula Mean?

- One of the definitions of the *mean* was that it always made the sum of the scores minus the mean equal to 0
- Thus, the average of the deviates must be 0 since the sum of the deviates must equal 0
- To avoid this problem, statisticians square the deviate score prior to averaging them
 - Squaring the deviate score makes all the squared scores positive

What Does the Variance Formula Mean?

- Variance is the mean of the squared deviation scores
- The larger the variance is, the more the scores deviate, on average, away from the mean
- The smaller the variance is, the less the scores deviate, on average, from the mean

Standard Deviation

- When the deviate scores are squared in variance, their unit of measure is squared as well
 - E.g. If people's weights are measured in pounds, then the variance of the weights would be expressed in pounds² (or squared pounds)
- Since squared units of measure are often awkward to deal with, the square root of variance is often used instead
 - The standard deviation is the square root of variance

Standard Deviation

- Standard deviation = $\sqrt{\text{variance}}$
- Variance = standard deviation²

Computational Formula

- When calculating variance, it is often easier to use a computational formula which is algebraically equivalent to the definitional formula:

$$\sigma^2 = \frac{\sum X^2 - \frac{(\sum X)^2}{N}}{N} = \frac{\sum (X - \mu)^2}{N}$$

- ✚ σ^2 is the population variance, X is a score, μ is the population mean, and N is the number of scores

Computational Formula Example

X	X^2	$X-\mu$	$(X-\mu)^2$
9	81	2	4
8	64	1	1
6	36	-1	1
5	25	-2	4
8	64	1	1
6	36	-1	1
$\Sigma = 42$	$\Sigma = 306$	$\Sigma = 0$	$\Sigma = 12$

Computational Formula Example

$$\sigma^2 = \frac{\sum X^2 - \frac{(\sum X)^2}{N}}{N}$$

$$= \frac{306 - \frac{42^2}{6}}{6}$$

$$= \frac{306 - 294}{6}$$

$$= \frac{12}{6}$$

$$= 2$$

$$\sigma^2 = \frac{\sum (X - \mu)^2}{N}$$

$$= \frac{12}{6}$$

$$= 2$$

Variance of a Sample

- Because the sample mean is not a perfect estimate of the population mean, the formula for the variance of a sample is slightly different from the formula for the variance of a population:

$$S^2 = \frac{\sum (X - \bar{X})^2}{N - 1}$$

- ⊕ s^2 is the sample variance, X is a score, \bar{X} is the sample mean, and N is the number of scores